# New Observational Constraints to MW Chemodynamical models

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# Milky Way Assembly & Evolution



Turon, Primas, Binney, Chiappini, Drew, Helmi, Robin, Ryan 2008

GREAT Chemo-dynamical Survey 2010, C. Babusiaux, A. Bragaglia, A. Brown, C. Chiappini, S. Feltzing, U. Heiter, A. Helmi, V. Hill, A. Lanzafame, A. Recio-Blanco, N. Walton The mechanism of formation and evolution of the Milky Way are encoded in the location, kinematics and chemistry of its stars



Galaxy shaped by several processes: gas accretion & chemical enrichment, mergers, radial migration

Are they all important? Which one dominates? When?

# **1. Need for Infall** The D Evolution

### Deuterium destroyed in stellar interiors



Its quantity in the ISM decreases from its primordial value to the current values measured recently by FUSE



Big Bang Nucleosynthesis



Before WMAP: Measuring primordial abundances of <sup>4</sup>He, D, <sup>3</sup>He and <sup>7</sup>Li to constrain the cosmic baryon density After WMAP: We know primordial abundances

### Infall needed to explain D/H and the metallicity distribution of long living stars

$$f = A \exp(-t/\tau)$$

G-dwarf Problem: Simple model and/or fast accretion predicts too many metal poor stars, not observed



# **2. Discontinuity in the Abundance Ratios**



Lack of scatter (10000 lower than metallicity range!)

Halo, Thick disk, Thin disk: cannot have been made by uncorrelated systems Suggestions of an age gap between thick disk and oldest stars in thin disk (Chiappini et al. 1997; Liu & Charboyer 2000, Sandage et al. 2003, Bernkopf & Furhmann 2006)



This behaviour is expect to show up more clearly for a ratio between an element restored on long timescales to the ISM (e.g. Fe, C) and an element ejected in short timescales (e.g. O)

(Chiappini et al. 2003 a,b)

# AMR from thin + thick

'This chemical map portrays the imprint of a huge SF gap" (Fuhrmann 2011)





# **Thick Disk** $f = A \exp(-t/\tau)$

 $\tau < 0.4 \text{ Gyr}$ 



## **Thin Disk**

 $f = A \exp(-t/\tau)$  $\tau (R_sun) = 7 Gyr$ 

#### Dispersion increases with ages: Age errors + mix populations (radial mixing + thick/thin stars) contribute to flattening/scatter



Da Silva et al. 2006: Giants – good for young ages/ larger errors for old ages scatter 0.1 dex = errors in last 4 Gyrs – mild CE last 4.5 Gyrs

Soubiran et al. 2007: Clump stars - tried to avoid thick disk stars (only thin) AMR less flat at old ages

### Predicted SN rates







We see stars here that are not born here Stars more metal rich than young stars & ISM

**Stellar Migration** 









# Open questions:

- Biased HR samples -> is gap real?
- Could radial migration alone make thick disk? And is the apparent "gap" just an effect of SNIa/SNII timescales + migration ? (Schoenrich & Binney 2009)
- > AMR flat + scatter due to radial migration (SB, and others)

# How to proceed?

Answers require work in two directions:

A. Unbiased samples (large ones, for larger volumes)

**B**. Chemodynamical model (within the cosmological framework) to see what is possible in terms of thick disk formation and if one simple disk can produce a gap in the abundance diagrams.

# A Leaving the Hipparcos volume...



Spectrophotometric Distances – Uncertainties ~ 20-30% (Santiago, Brauer, Anders, Chiappini et al. 2014 Schultheis et al. 2014; Binney et al. 2014) APOGEE Red Clump Catalog – Uncertainties ~10 % (Bovy et al 2014, submitted)

# More constraints with RAVE + SEGUE

#### RAVE SEGUE SEGUE-2

Moderate – low resolution



RAVE giants (red) sample a similar volume as SEGUE dwarfs (black)

Boeche, Chiappini + RAVE collaboration 2013, MNRAS Brauer, Chiappini, + SDSSIII-BPG (in preparation) Minchev, Chiappini, Martig + RAVE collaboration 2014, ApJ Letters Boeche et al. 2013, 2014 (RAVE gradients dwarfs & giants)

#### RAVE – individual abundances -First time that abundance gradients to such a large dataset!



Discrepancy caused by the lack of correlation between metallicity and tangential velocity (or angular momentum) in models (e.g. Besancon, Trilegal).



#### Chemodynamics of the Milky Way

A&A 564, A115 (2014)

#### I. The first year of APOGEE data\*

F. Anders<sup>1,2</sup>, C. Chiappini<sup>1,3</sup>, B. X. Santiago<sup>3,4</sup>, H. J. Rocha-Pinto<sup>3,5</sup>, L. Girardi<sup>3,6</sup>, L. N. da Costa<sup>3,7</sup>, M. A. G. Maia<sup>3,7</sup>, M. Steinmetz<sup>1</sup>, I. Minchev<sup>1</sup>, M. Schultheis<sup>8</sup>, C. Boeche<sup>9</sup>, A. Miglio<sup>10</sup>, J. Montalbán<sup>11</sup>, D. P. Schneider<sup>12,13</sup>, T. C. Beers<sup>14,15</sup>, K. Cunha<sup>7,16</sup>, C. Allende Prieto<sup>17</sup>, E. Balbinot<sup>3,4</sup>, D. Bizyaev<sup>18</sup>, D. E. Brauer<sup>1</sup>, J. Brinkmann<sup>18</sup>, P. M. Frinchaboy<sup>19</sup>, A. E. García Pérez<sup>20</sup>, M. R. Hayden<sup>21</sup>, F. R. Hearty<sup>20,12</sup>, J. Holtzman<sup>21</sup>, J. A. Johnson<sup>22</sup>, K. Kinemuchi<sup>18</sup>, S. R. Majewski<sup>20</sup>, E. Malanushenko<sup>18</sup>, V. Malanushenko<sup>18</sup>, D. L. Nidever<sup>23</sup>, R. W. O'Connell<sup>20</sup>, K. Pan<sup>18</sup>, A. C. Robin<sup>24</sup>, R. P. Schiavon<sup>25</sup>, M. Shetrone<sup>26</sup>, M. F. Skrutskie<sup>20</sup>, V. V. Smith<sup>14</sup>, K. Stassun<sup>27</sup>, and G. Zasowski<sup>28</sup>



#### APOGEE Gradients & MDF (raw)



Anders, Chiappini et al. 2014

# Gaia ESO - UVES

#### Bergmann et al. 2014

- 144 stars
- ages 0.5 13.5 Gyr
- 6 < R (kpc) < 9
- 0 < |Z| < 1.5 kpc



# Asteroseismology: Constraints at larger distances!

# CoRot & Kepler



LRc01

-15000

-10000

x (pc)

-5000

Crucial role played by solar-like pulsating RGs:

- well-populated class of accurate distance indicators
- spanning a large age range
- probe large distances

Distances and age

alactic Centr

0

$$\frac{M}{M_{\odot}} \simeq \left(\frac{\nu_{\max}}{\nu_{\max,\odot}}\right)^{3} \left(\frac{\Delta\nu}{\Delta\nu_{\odot}}\right)^{-4} \left(\frac{T_{\text{eff}}}{T_{\text{eff},\odot}}\right)^{3/2}$$
$$\frac{R}{R_{\odot}} \simeq \left(\frac{\nu_{\max}}{\nu_{\max,\odot}}\right) \left(\frac{\Delta\nu}{\Delta\nu_{\odot}}\right)^{-2} \left(\frac{T_{\text{eff}}}{T_{\text{eff},\odot}}\right)^{1/2}.$$

- ullet Uncertainty on M  $\sim 10\%$
- $\bullet~$  Uncertainty on R  $\sim 3\%$

# Stepping out with Asteroseismology

■ Uncertainties in distances ~ 15 %; <5% for high quality data

$$egin{aligned} \log d &= 1+2.5\lograc{T_{ ext{eff}}}{T_{ ext{eff},\odot}}ert \lograc{
u_{ ext{max}}}{
u_{ ext{max},\odot}} + \ &-2\lograc{\Delta
u}{\Delta
u_{\odot}} + 0.2(m_{ ext{bol}}-M_{ ext{bol},\odot}), \end{aligned}$$

*d* is expressed in pc,  $m_{bol}$  = apparent bolometric magnitude,  $M_{bol,\odot}$  = absolute solar bolometric magnitude.

Seismic log g -> uncertainty of 0.03 dex [spectroscopic usually 0.1-0.3 dex!]

$$\log g = \log g_{\odot} + \log \left(\frac{\nu_{\max}}{\nu_{\max,\odot}}\right) + \frac{1}{2} \log \left(\frac{T_{\text{eff}}}{T_{\text{eff},\odot}}\right)$$

### CoRoT

First use of asteroseismology to determine precise distances for a large (~2000) sample of field stars (giants) spread across nearly 15 kpc of the Galactic disc, exploring regions which are a long way from the solar neighbourhood.





y (pc)

Miglio, Chiappini, Morel, Barbieri, Chaplin, Girardi, Montalban, Noels, Valentini, Mosser, Baudin, Casagrande, Fossati, Silva Aguirre & Baglin 2013, MNRAS 429, 423 [LRa01+Lrc01 analysis]



We find significant differences in the mass distributions of these two samples which, by comparison with predictions of synthetic models of the Milky Way (TRILEGAL), we interpret as mainly due to the vertical gradient in the distribution of stellar masses (hence ages) in the thin disc.



Age Distances

On going follow up of LRa01 by APOGEE;

LRc01 by GAIA-ESO,

observations – some

with RAVE info

Kepler targets by

APOGEE

More Kepler

### Gaia

Asteroseismology (CoRoT & Kepler & PLATO) Mass, Radius & Evolutionary Stage

ne Structure

2 Spring

Stellar parameters, metallicities [alpha/Fe] and detailed abundances

### Ground-based spectroscopic Surveys needed

- APOKASC -> Extinctions & distances for ~2000 stars; • 0.5 < d (kpc) < 5kpc; Current uncertainty < 2% ! (Rodrigues et al. 2014 – BPG/SDSSIII – in preparation)
- CoRoT follow-up with Gaia-ESO -> data in hands UVES • + FLAMES-GIRAFFE – Valentini et al. - in preparation)

Workshop: "Reconstructing the Milky Way's history: spectroscopic Surveys, Asteroseismology and chemodynamical models", June 1-5 2015 Physics Center Bad Honnef - Bonn – Germany

# Chemodynamical models

N-body Simulations: Why?

 N-body simulations are the appropriate technique to treat timedependent non-axisymmetric systems such as our barred galaxy

A

- 3D self-gravitating systems with large dynamic range in temporal scales, involving both gas and collisionless matter (stars) TreeSPH codes, AMR, Voronoi
- Gas Increases complexity due to star formation and energy feedback
   Chemistry/Mass return
- The role of the bar in radial migration cannot be ignored (Minchev et al. 2010, Brunetti, Chiappini & Pfenniger 2011)

**Caveat:** non-physical effects (e.g. overcooling, overmerging, angular momentum loss) when trying to describe sub-grid physics governing galaxy evolution (Star formation, feedback, magnetic fields..)

# New Approach "Surrogate galaxies"

Minchev, Chiappini, Martig 2013 I. A&A 558, id.A9 (MCM Model) Minchev, Chiappini, Martig 2014 II. A&A (submitted)

- Choose a high-resolution simulation in the cosmological framework that meet the following MW properties :
- ➢ a bar
- gas accretion disk grows inside-out (gas from filaments + mergers)
- early mergers merger activity decreases toward redshift zero
- ➢ lasts for at least 10 Gyrs
- Disk Properties at redshift zero => consistent with dynamics & morphology of MW: Presence of a MW size bar; small bulge
- We place the "solar radius" (8 kpc) just outside the 2:1 outer Lindblad resonance (OLR) of the bar, as is believed to be the case for the MW (e.g., Dehnen 2000; Minchev et al. 2007)
- We resample the disk's SFH appropriate for the chemical evolution model
- Use a pure thin disk chemical evolution model (from the point of view of star formation history) the simplest case, no SFR threshold, no pre-enrichment
- We extract self-consistent dynamics: radial migration from internal perturbations + mergers

# Input Dynamics Martig et al. 2012



We can now look for the contamination (from migration) to the input chemical model

# Input Chemistry

### **Pure Thin Disk** Solar Vicinity



Matching several observational constraints in the MW, some of them not affected by migration (e.g., deuterium)

### **Pure Thin Disk**



Using  $\tau(r)$  from Chiappini et al. 2001 But assuming something "ad hoc" for r < 4 kpc (in this region, not clear what happens to abundance gradients/bulge)

# Metallicity Distribution at Solar Vicinity Mosaic of stars born at different $R_{initial}$ at different times $r_0 = Birth Radii in kpc$





# Radial migration produces scatter in AMR But some trend is preserved

(the mean is close to the R=8kpc curve – cyan)



### Strong radial migration – but not much scatter in [O/Fe]



AGES!

## Close look at properties of the oldest population (red):

Is this the Thick disk?????

- Have thick disk like ages
- Have thick disk like MDF
- Have thick disk like [O/Fe]
- Lag the "thin disk" by ~50 km/s



AGES!

### RAVE

### MCM MODEL



# The properties at different places in the disk The R<sub>birth</sub> mix

Stars that today are in the indicated bin, came from different R0

Minchev, Chiappini, Martig 2014, A&A (submitted) – MCM II



#### 1.0 3<r<5 kpc 5<r<7 kpc 7<r<9 kpc 9<r<11 kpc 11<r<13 kpc z < 3 kpc

0.8



"high-alphas" contribution decreases towards outer disk

# The properties at different places in the disk: AMR



### **Gradients – Model Prediction**





### Selection effects can create discontinuity in [O/Fe] plot



Probability membership to either "Thick" and "Thin" velocity ellipsoids

Is the bimodality in the [Fe/H]-[O/Fe] plane due to selection effects?





→ −0.4 −0.2 [M/H]







### If not all samples are biased, is the gap real?!

Fuhrmann 2011



Figure 15. The local, volume-complete perspective on the magnesium and iron abundances of 271 F-, G- and K-type stars. Upper panel: [Mg/Fe] versus [Fe/H]; lower panel: the same data, but with the  $\alpha$ -chain element magnesium as reference. Circle diameters are in proportion to the stellar age estimates. This chemical map portrays the imprint of a huge star formation gap that subdivides the extremely old ( $\tau \ge 12$  Gyr) thick-disc stars in a fairly flat abundance distribution from the much younger and well-displaced thin-disc stars ( $\tau \le 8$  Gyr) in a curved string-of-pearl-like distribution. Only five objects dubbed as transition stars display intermediate characteristics.

# and with Gaia & 4MOST...



PI. R. de Jong (AIP)

Chiappini: Project Scientist (2011-2013) Now: Sofia Feltzing + Richard MacMahom

Chiappini et al. 2013, Science Report (~90pp)

- 4MOST Phase A Review (May 2013); Approved for Phase B (mid-2013)
- First light 2020 -> > 10 million targets in the disk!

# Take home message:

#### **GOLD ERA FOR GALACTIC ARCHAEOLOGY: NEAR FIELD COSMOLOGY**

- Stars observed "here" are combination of stars born hot + radial migration bringing contribution of old stars from inner radii
- The MW "thick disc" emerges naturally from (i) stars born with high velocity dispersions at high redshift, (ii) stars migrating from the inner disc early on due to strong merger activity, and (iii) further radial migration driven by the bar and spirals at later times
- The older population has the properties of what has been called "thick disk", but not a clear gap in chemical plane
- If you apply to the particles similar "observational biases" you get chemical discontinuity, but there are samples that seem to be free of biases and still show a gap! (e.g. Fuhrmann's, Gaia-ESO, HARPS, APOGEE)
- For now we are using [alpha/Fe] as proxy for age. Tighter constraints will come once we could use ages, even just in large bins (asteroseismology)
- Plan: to use all these new constraints to improve models, make mocks with the N-body simulation as "seen" by the different surveys

Workshop: "Reconstructing the Milky Way's history: spectroscopic Surveys, Asteroseismology and chemodynamical models", June 1-5 2015 Physics Center Bad Honnef - Bonn – Germany



# EXTRAS

### RAVE

### MCM MODEL





These findings can be explained by perturbations from massive mergers in the early Universe and the subsequent radial migration of stars with cooler kinematics from the inner disc:

During mergers (early on) stars migrating outwards arrive significantly colder than the in-situ population

# How much enrichment from $t_{sun}$ to $t_{now}$ ?

Table 5: Comparison of the proto-solar abundances from the present work and Grevesse & Sauval (1998) with those in nearby B stars and HII regions. The solar values given here include the effects of diffusion (Turcotte & Wimmer-Schweingruber 2002) as discussed in Sect. 3.11. The HII numbers include the estimated elemental fractions tied up in dust; the dust corrections for Mg, Si and Fe are very large and thus too uncertain to provide meaningful values here. Also given in the last column is the predicted Galactic chemical enrichment (GCE) over the past 4.56 Gyr.

						L
Elem.	$Sun^a$	$Sun^b$	$B \text{ stars}^c$	$\mathrm{H II^d}$	GCE <sup>e</sup>	
He	$10.98 \pm 0.01$	$10.98\pm0.01$	$10.98\pm0.02$	$10.96 \pm 0.01$	0.01	
С	$8.56 \pm 0.06$	$8.46 \pm 0.05$	$8.32\pm0.03$	$8.66 \pm 0.06$	0.06	
Ν	$7.96 \pm 0.06$	$7.87 \pm 0.05$	$7.76\pm0.05$	$7.85\pm0.06$	0.08	
0	$8.87 \pm 0.06$	$8.74\pm0.05$	$8.76\pm0.03$	$8.80\pm0.04$	0.04	
Ne	$8.12\pm0.06$	$7.98 \pm 0.10$	$8.08\pm0.03$	$8.00\pm0.08$	0.04	Γ
Mg	$7.62\pm0.05$	$7.62\pm0.04$	$7.56\pm0.05$		0.04	
Si	$7.59 \pm 0.05$	$7.55\pm0.04$	$7.50\pm0.02$		0.08	
S	$7.37\pm0.11$	$7.19\pm0.04$	$7.21\pm0.13$	$7.30\pm0.04$	0.09	
Ar	$6.44\pm0.06$	$6.44 \pm 0.13$	$6.66 \pm 0.06$	$6.62\pm0.06$		
Fe	$7.55\pm0.05$	$7.55\pm0.04$	$7.44\pm0.04$		0.14	

<sup>a</sup> Grevesse & Sauval (1998) <sup>b</sup> Present work <sup>c</sup> Przybilla, Nieva & Butler (2008), Morel et al. (2006), Lanz et al. (2008) <sup>d</sup> Esteban et al. (2005, 2004), García-Rojas & Esteban (2007) <sup>e</sup> Chiappini, Romano & Matteucci (2003).

Asplund et al. 2009

#### Chemical gradients in the Milky Way from the RAVE data I. Dwarf stars A&A 559, A59 (2013) C. Boeche<sup>1,2</sup>, A. Siebert<sup>3</sup>, T. Piffl<sup>2</sup>, A. Just<sup>1</sup>, M. Steinmetz<sup>2</sup>, S. Sharma<sup>4</sup>, G. Kordopatis<sup>5</sup>, G. Gilmore<sup>5</sup>, C. Chiappini<sup>2</sup>, M. Williams<sup>2</sup>, E. K. Grebel<sup>1</sup>, J. Bland-Hawthorn<sup>4</sup>, B. K. Gibson<sup>6,7</sup>, U. Munari<sup>8</sup>, A. Siviero<sup>9,2</sup>, O. Bienaymé<sup>3</sup>, J. F. Navarro<sup>10</sup>, O. A. Parker<sup>11,12,13</sup>, W. Reid<sup>12</sup>, G. M. Seabroke<sup>14</sup>, F. G. Watson<sup>13</sup>, R. F. G. Wyse<sup>15</sup>, and T. Zwitter<sup>16,17</sup> Gradients flatten with height above plane RAVE 60 Service Control States in Zmax (kpc)>0.8 0 [Fe/H] 40 20 -2 N= 399 = d[X/H]/dRg= 0.006 0 -3 0.4 <Zmax (kpc)<0.8 0 400 [Fe/H] 200 -2 $d[X/H]/dR_{q} = -0.059$ N= 3032 = 0 -33000 0.0 <Zmax (kpc)<0.4 0 Fe/H] 2000 1000 -2 $d[X/H]/dR_{g} = -0.065$ N=16456= 0 -3

R<sub>g</sub> (kpc)

6

8

-1.0

-0.5

0.0

0.5

-1.5

#### Mock Sample – with GALAXIA-Besancon

These huge datasets offer important constraints both for synthetic models and chemodynamical models But in synthetic models -> lack correlation between chemistry and kinematics





[Fa/H] [Fa/H] [Fa/

#### Mock Sample – with GALAXIA-Besancon



Table 3. Radial [Fe/H]<sup>*a*</sup> gradients with respect to the orbital guiding radius<sup>*b*</sup> in the range  $6 < R_g < 11$  kpc, for four ranges of  $z_{max}$ .

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$\frac{d[Fe/H]}{dR_g}$ [dex/kpc]	APOGEE HQ <sup>k</sup>	APOGEE Gold	GCS dwarfs <sup>c</sup>	RAVE dwarfs <sup>a</sup>
$0.0 \le z_{max} [kpc] < 0.4$	$\begin{array}{c} -0.066 \pm 0.006 \\ -0.041 \pm 0.004 \\ +0.000 \pm 0.004 \\ +0.052 \pm 0.004 \end{array}$	$-0.074 \pm 0.010$	$-0.043 \pm 0.004$	$-0.065 \pm 0.003$
$0.4 \le z_{max} [kpc] < 0.8$		$-0.038 \pm 0.008$	$-0.008 \pm 0.011$	$-0.059 \pm 0.005$
$0.8 \le z_{max} [kpc] < 1.5$		$+0.026 \pm 0.008$	$+0.056 \pm 0.019$	$+0.006 \pm 0.015$
$1.5 \le z_{max} [kpc] < 3.0$		$+0.049 \pm 0.008$	-	-

Table 4. Radial  $[\alpha/\text{Fe}]^a$  gradients with respect to the orbital guiding radius<sup>*b*</sup> in the range 6 <  $R_g$  < 11 kpc, for four ranges of  $z_{\text{max}}$ .

$\frac{d[\alpha/Fe]}{dR_g}$ [dex/kpc]	APOGEE HQ <sup>k</sup>	APOGEE Gold	GCS dwarfs <sup>c</sup>	RAVE dwarfs <sup>a</sup>
$0.0 \le z_{\rm max}  [\rm kpc] < 0.4$	$-0.005 \pm 0.001$	$-0.005 \pm 0.002$	$+0.010 \pm 0.002$	$-0.004 \pm 0.001$
$0.4 \le z_{\rm max}  [\rm kpc] < 0.8$	$-0.009 \pm 0.001$	$-0.007 \pm 0.002$	$-0.006 \pm 0.005$	$-0.005 \pm 0.002$
$0.8 \le z_{max} [kpc] < 1.5$	$-0.019 \pm 0.001$	$-0.022 \pm 0.002$	$-0.023 \pm 0.007$	$-0.020 \pm 0.005$
$1.5 \le z_{\rm max}  [\rm kpc] < 3.0$	$-0.031 \pm 0.001$	$-0.023 \pm 0.002$	-	_



#### RAVE GIANTS – Boeche et al. 2014 (submitted)

	$\frac{d[Fe/H]}{dZ}$	$\frac{d[Mg/H]}{dZ}$	$\frac{d[Al/H]}{dZ}$	$\frac{d[Si/H]}{dZ}$	$\frac{d[Ti/H]}{dZ}$	$\frac{d[Fe/H]}{dZ}$ (mock)
$0.0 <  Z  (kpc) \le 0.4$ $0.4 <  Z  (kpc) \le 0.8$ $0.8 <  Z  (kpc) \le 1.2$ 1.2 <  Z  (kpc) < 2.0	$\begin{array}{c} -0.050 \pm 0.027 \\ -0.087 \pm 0.030 \\ -0.148 \pm 0.073 \\ -0.199 \pm 0.070 \end{array}$	$+0.019 \pm 0.022$ +0.022 $\pm 0.025$ -0.031 $\pm 0.061$ +0.041 $\pm 0.096$	$+0.045 \pm 0.030$ $-0.027 \pm 0.034$ $-0.124 \pm 0.075$ $+0.031 \pm 0.104$	$-0.088 \pm 0.030$ $-0.117 \pm 0.033$ $-0.197 \pm 0.078$ $-0.140 \pm 0.096$	$+0.081 \pm 0.023$ $+0.076 \pm 0.023$ $+0.010 \pm 0.055$ $-0.086 \pm 0.068$	$\begin{array}{c} -0.373 \pm 0.031 \\ -0.409 \pm 0.038 \\ -0.536 \pm 0.085 \\ -0.338 \pm 0.083 \end{array}$

	$\frac{d[Fe/H]}{dR}$	$\frac{d[Mg/H]}{dR}$	$\frac{d[Al/H]}{dR}$	$\frac{d[Si/H]}{dR}$	$\frac{d[Ti/H]}{dR}$	$\frac{d[Fe/H]}{dR}$ (mock)
$0.0 <  Z  (\text{kpc}) \le 0.4$	$-0.054 \pm 0.004$	$-0.034 \pm 0.004$	$-0.035 \pm 0.005$	$-0.064 \pm 0.005$	$+0.008 \pm 0.004$	$-0.049 \pm 0.006$
$0.4 <  Z  (kpc) \le 0.8$	$-0.039 \pm 0.004$	$-0.031 \pm 0.004$	$-0.032 \pm 0.005$	$-0.046 \pm 0.004$	$-0.005 \pm 0.003$	$-0.019 \pm 0.005$
$0.8 <  Z  (kpc) \le 1.2$	$-0.011 \pm 0.008$	$-0.023 \pm 0.007$	$-0.027 \pm 0.009$	$-0.028 \pm 0.008$	$-0.015 \pm 0.006$	$+0.030 \pm 0.009$
1.2 <  Z  (kpc)< 2.0	$+0.047 \pm 0.018$	$+0.025 \pm 0.015$	$+0.060 \pm 0.022$	$+0.009 \pm 0.018$	$+0.032 \pm 0.017$	$+0.061 \pm 0.012$



